

# Concurrency Effects Over Variable-size Identifiers in Distributed Collaborative Editing

ConcoRDanT

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# LSEQ, an allocation strategy for variable-size CRDTs

## All is about the insert operation

- $\text{insert}(id_p, \text{element}, id_q) \Rightarrow \text{alloc}(id_p, id_q) \Rightarrow id_{\text{element}}$  such as  $id_p < id_{\text{element}} < id_q$

## Allocation strategy before

- *linear*
- *editing behaviour dependant*  $\Rightarrow$  design for end-editing

0

1

9

A

## LSEQ allocation strategy

- lowered the space complexity : linear  $\Rightarrow$  polylogarithmic
- any editing behaviour
  - $\Rightarrow$  variable-size CRDTs safe
  - $\Rightarrow$  avoids additional protocol
  - $\Rightarrow$  ready to use in editors?

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0	1	4	9
	A	N	

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0	1	4	7	8	9
	A	N	G	E	S

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	A	N	G	E	S	

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## Allocation strategy before

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0	0.1	1	4	7	8	8.1	9
	H	A	N	G	E	S	

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	C	H	A	N	G	E	S	

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0	etc...	0.0.1	0.1	1	4	7	8	8.1	9
		D	C	H	A	N	G	E	S

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# Not yet...

left open in LSEQ perspectives : the **concurrency effects**

- how the LSEQ **alloc** function behaves when

- 1 varying number of users
- 2 varying latency

	#insert operations				
	10	100	200	500	1000
1 user (bit/id)	6.5	26.8	32.7	56.0	64.2
10 users (bit/id)	9.5	125.8	377.0	1962.1	5468.0

- expectation : sub-linear behaviour
- reality : quadratic growth

⇒ only **partially** improves variable-size identifiers

# Objective

- Solve the limitation of LSEQ in context involving concurrency
  - **Extends** sub-linear upper-bound of single user to **multiple users**
  - **Study** the effect of **latency** over the size of identifiers
- ⇒ No costly additional protocol
- ⇒ I can build a Distributed Collaborative Editor based on variable-size CRDTs
  - Decentralized
  - Simple algorithms
  - Tiny metadata

# Proposal : h-LSEQ

## Similar to LSEQ

- exponential tree model
- multiple sub allocation strategies
  - designed for end-editing
  - designed for front-editing

## Different

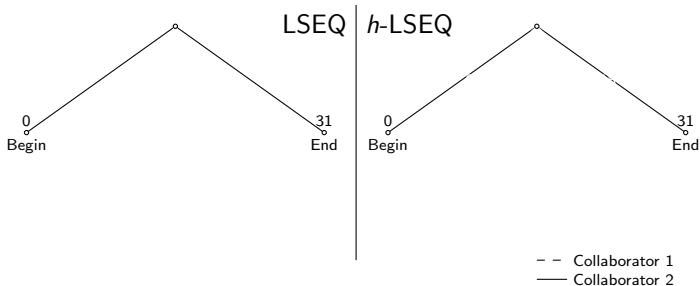
- strategy choice

	local	different
LSEQ	random	different
<i>h</i> -LSEQ	random	<b>similar</b>

## Intuition

The shared hash function provide an *a priori* **agreement** over participants on which strategy to employ. This agreement **avoids** the possibility of **antagonist choices** which would have led to a bad global allocation of identifiers.

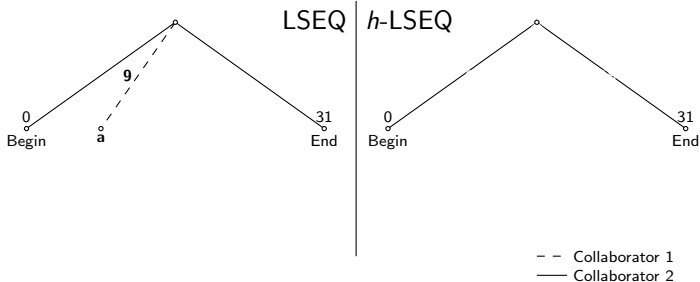
# LSEQ vs *h*-LSEQ : example



- 1 user1 : insert(B,a,E)  
⇒ lvl 1 → End-editing  
⇒ [9]
- 2 user2 : insert(a,b,E)  
⇒ lvl 1 → Front-editing  
⇒ [30]
- 3 repeat 1 x : depth increases
- 4 repeat n x : quadratic growth

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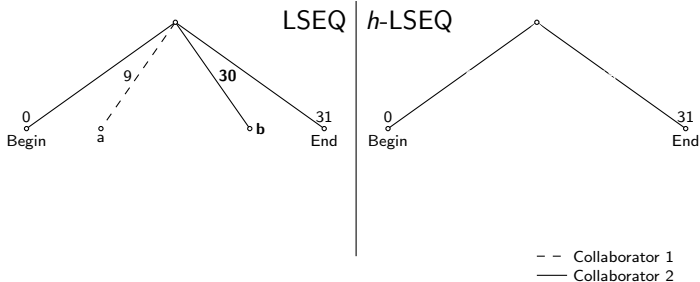
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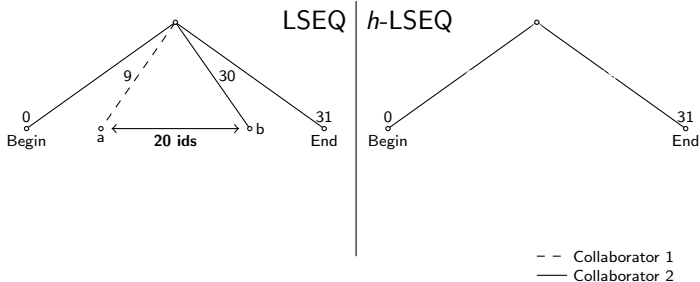
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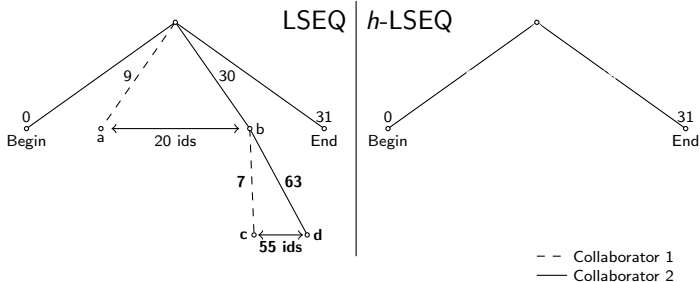
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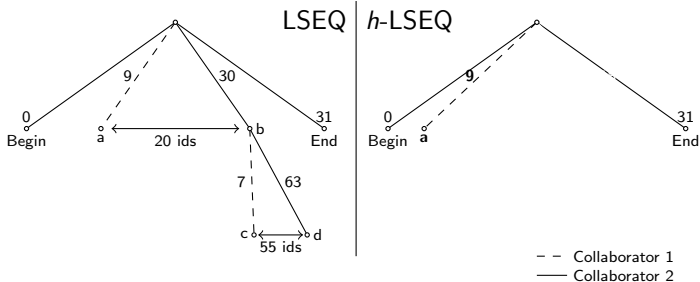


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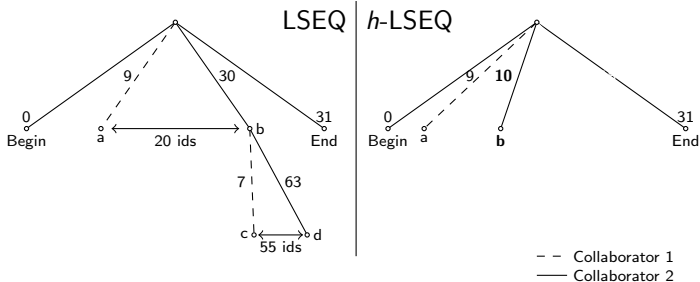
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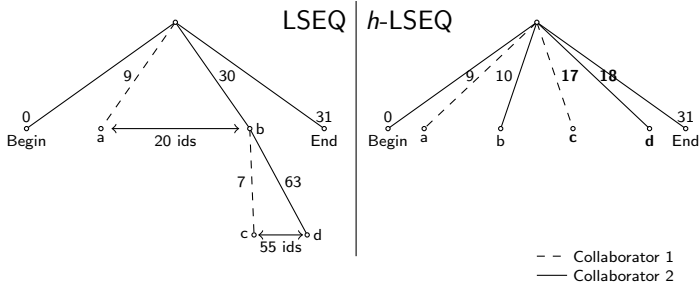
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# Experiments

## 1 Evaluation of LSEQ and $h$ -LSEQ on a collaboration involving **multiple users**

- ⇒ Synthetic documents (100 lines)
- ⇒ 10 users (10 op/each)
- ⇒ Editing behaviour : end editing
- ⇒ Instant delivery of messages ( $\approx$  LAN)

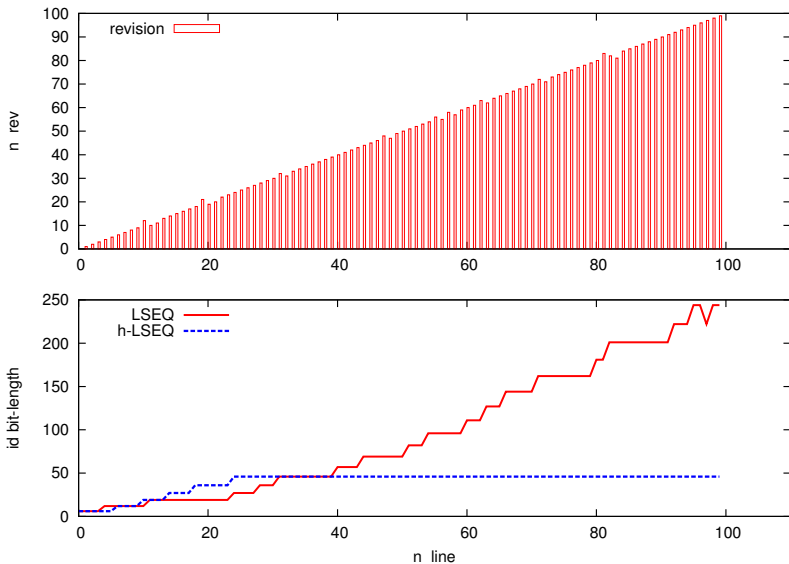
Expect :    **a** LSEQ  $\Rightarrow$  quick growth of identifiers  
              **b**  $h$ -LSEQ  $\Rightarrow$  quick stabilization  $\Rightarrow$  sub-linear upper-bound

## 2 Evaluation of LSEQ and $h$ -LSEQ with **varying latency**

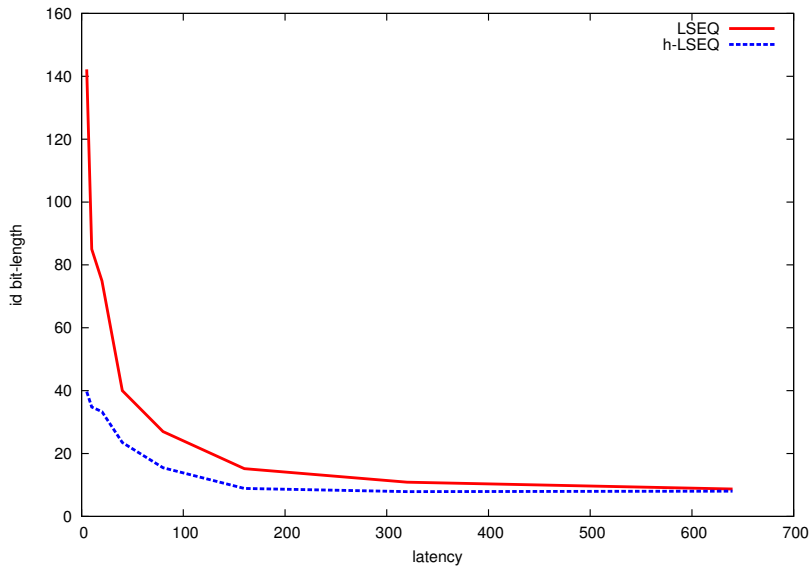
- ⇒ Synthetic documents (100 lines)
- ⇒ 10 users (10 op/each)
- ⇒ Editing behaviour : end editing

Expect :    **a** no latency : worst-case  
              **b** latency  $\nearrow$  then  $\text{avg}(\text{id.size}) \searrow$

## $h$ -LSEQ scales in term of users



# Latency does not badly impact variable-size CRDTs



# Synthesis : experiments

- 1  $h$ -LSEQ  $\Rightarrow$  hash-based choice strategy  $\Rightarrow$  global agreement on employed strategies
    - $\Rightarrow$  No additionnal cost (only a shared seed within the document)
    - $\Rightarrow$  Generalize the space complexity from single user to multiple users
  - 2 Latency :
    - No bad impact on size of identifiers
    - No latency  $\Rightarrow$  upper-bound on the size of identifiers
- $\Rightarrow$   $h$ -LSEQ supports concurrency

# Conclusion

$h$ -LSEQ handles concurrency

⇒ limitation solved

With  $h$ -LSEQ :

- Distributed Collaborative Editors
  - Decentralized
  - Very simple algorithms
  - tiny metadata

*CRDT-based distributed collaborative editors using  $h$ -LSEQ constitutes a good alternative to trending editors such as Google Docs, Etherpad... with better scalability.*



# Future works

- 1 Develop the Distributed Collaborative Editor
- 2 Proof
  - $n$  operations : uniform distribution  $\Rightarrow O((\log \log n)^2)$
  - $n$  operations : monotononic  $\Rightarrow O((\log n)^2)$
  - $n$  operations : worst-case  $\Rightarrow O(n^2)$
- 3 Proof : worst-case happens with a negligible probability
- 4 Causality tracking (still an issue in distributed systems with churn)
  - does not scale in term of user
  - or does not provide exact causality $\Rightarrow$  CRDTs for sequences require causality...

**Thank you !**